Spin and isospin effects in the NN \rightarrow NKA reaction near threshold

G. Fäldt^{1,a} and C. Wilkin^{2,b}

¹ Department of Radiation Sciences, Box 535, S-751 21 Uppsala, Sweden

 $^2\,$ Department of Physics & Astronomy, UCL, London WC1E 6BT, UK

Received: 5 November 2004 / Revised version: 7 February 2005 / Published online: 20 May 2005 – © Società Italiana di Fisica / Springer-Verlag 2005 Communicated by A. Molinari

Abstract. The spin and isospin structure of the amplitudes and observables for $K^+\Lambda$ production in nucleonnucleon collisions in the near-threshold region is analysed. Five experiments are required in order to isolate the amplitudes, up to an overall phase and two discrete ambiguities, in a model-independent way. It is shown that, with reasonable values for the relative strengths of the π and ρ terms in a meson-exchange model, one expects production on the neutron to be significantly stronger than that on the proton. Negative values of the spin-transfer coefficient D_{NN} are also predicted due to π - ρ interference.

PACS. 13.60.Le Meson production – 14.40.Aq π , K, and η mesons – 13.75.Ev Hyperon-nucleon interactions – 13.88.+e Polarization in interactions and scattering

1 Introduction

The study of meson production near threshold in nucleonnucleon scattering has been a growth area over the last decade and most of the modelling of experimental data has been in terms of some form of meson-exchange model [1, 2]. The energy dependence of the total cross-section is generally dominated by phase-space, folded with a strong nucleon-nucleon final-state interaction (fsi) [3]. The information that the data give on the basic driving term is therefore very limited and has to be supplemented by results from angular distributions and Dalitz plots, etc. A particularly valuable constraint on theoretical models is the relative strength of the production in neutron-proton and proton-proton collisions. For η production, it is found that $\mathcal{R}(\eta) = \sigma(pn \to \eta pn) / \sigma(pp \to \eta pp) = 6.5 \pm 1.0$ [4]. Neglecting the differences between the np and pp initialand final-state interactions, the exchange of just a single pion or ρ -meson would lead to a factor of 5 [5], which is close to the experimental value. This is reduced by the fsi, but a quantitative agreement with the observables can be obtained with ρ -meson exchange being more important than that of the π [6], though alternative scenarios are in the literature [7,8].

The COSY11 [9,10] and COSY-TOF [11,12] Collaborations have made measurements in proton-proton collisions of both $K^+\Lambda$ and $K\Sigma$ production near their respective production thresholds. The excitation functions look broadly similar to those for reactions such as $pp \to pp\eta$, though the effects of the final-state interaction are somewhat less because the hyperon-nucleon scattering lengths are much smaller than that in pp. Though proton-neutron data are much more sparse, there are strong indications from reactions on deuterium that $\mathcal{R}(K^+)$ is also significantly over unity [13]. It is the purpose of this paper to explore whether a large value of $\mathcal{R}(K^+)$ could be understood within a meson-exchange model and to see what consequences this might have for the spin dependence of the production process.

The $pp \to pK^+\Lambda$ cross-section near threshold has been estimated by several groups [14–18], but there is no general consensus as to whether the reaction is driven mainly by the exchange of strange or non-strange mesons. In part, this is due to the tremendous uncertainty in the pKA coupling constant, as well as in the off-shell behaviour of the K^+p scattering amplitude, which is not resonance dominated. However, the recent results from COSY-TOF [12] clearly indicate that the Dalitz plots for $pp \to pK^+\Lambda$ are dominated by the excitation of nucleon isobars, though modified by the Ap fsi. At their lowest beam momentum (2.85 GeV/c) only the $N^*(1650)$ was seen but the $N^*(1710)$ becomes steadily more important as the momentum is raised. This suggests that strange meson exchange, which cannot excite such isobars, plays only a minor role in the process. Nevertheless, it is impossible as yet to estimate reliably the overall rate for the reaction, principally because of the uncertainty in the final Ap wave

^a e-mail: goran.faldt@tsl.uu.se

^b e-mail: cw@hep.ucl.ac.uk

function, especially at short distances. Different modern potentials that reproduce the limited scattering data give values of the singlet scattering length that vary from -0.71 fm to -2.51 fm [19]. We therefore limit ourselves to the evaluation of cross-section ratios, which depend far less on the distortion in the final, or initial state [8].

Only three amplitudes are necessary to describe $NN \rightarrow K\Lambda N$ near threshold, and their spin and isospin structure are identified in sect. 2, where cross-sections and spin observables are written in terms of them. Since there are more than five possible observables, there must be relations between some of them, and one of these is illustrated here. If one could measure production in pp and pn collisions, and the transverse spin correlation in either case, then one would be able to separate the contributions of spin-singlet and -triplet ΛN final states in a model-independent way.

To illustrate the sizes of possible effects, the contributions to the spin-isospin amplitudes are studied in sect. 3 within a meson-exchange model. Though strange and nonstrange exchanges are considered, detailed evaluation is confined to the case where only the π and ρ are important. As discussed in sect. 4, the energy dependence of the total cross-section is determined by the low-energy Apscattering parameters but the normalisation depends also upon the Ap interaction at short distances, which is largely unknown. The variation of $\mathcal{R}(K^+)$ with the π/ρ strength is shown in sect. 5. With the π/ρ ratio scaled from that used in the η case, significantly more $K^+\Lambda$ production is to be expected in pn than in pp collisions. Furthermore, the spin-transfer parameter might be large and negative through π - ρ interference, though neither π nor ρ alone lead to a negative value. Our conclusions are reported in sect. 6.

2 Amplitudes and observables

The most general structure of the isotriplet and singlet $NN \to NK\Lambda$ amplitudes near threshold is

$$\mathcal{M}_{1} = \left[W_{1,s} \eta_{f}^{\dagger} \, \hat{\boldsymbol{p}} \cdot \boldsymbol{\epsilon}_{i} + i W_{1,t} \, \hat{\boldsymbol{p}} \cdot (\boldsymbol{\epsilon}_{i} \times \boldsymbol{\epsilon}_{f}^{\dagger}) \right] \, \boldsymbol{\chi}_{f}^{\dagger} \cdot \boldsymbol{\chi}_{i} \,,$$
$$\mathcal{M}_{0} = W_{0,t} \, \hat{\boldsymbol{p}} \cdot \boldsymbol{\epsilon}_{f}^{\dagger} \, \eta_{i} \, \phi_{f}^{\dagger} \, \phi_{i} \,, \qquad (2.1)$$

where p is the incident c.m. beam momentum. The initial (final) baryons couple to spin-1 or spin-0, represented by ϵ_i (ϵ_f) and η_i (η_f), respectively [20]. Similarly, the χ_i (χ_f) and ϕ_i (ϕ_f) describe the isospin-1 and isospin-0 combinations of the initial NN (final KN) states.

The amplitudes $W_{1,s}$, $W_{1,t}$, and $W_{0,t}$ correspond to the transitions ${}^{3}P_{0} \rightarrow {}^{1}S_{0}s$, ${}^{3}P_{1} \rightarrow {}^{3}S_{1}s$, and ${}^{1}P_{1} \rightarrow {}^{3}S_{1}s$, respectively, in the partial-wave notation. It is important to note that, due to the Pauli principle, $W_{1,t} = 0$ for the analogous $pp \rightarrow pp\eta$ reaction. This vanishing leads to quite different spin and isospin effects for K and η production.

After a little spin algebra, it is seen that the unpolarised intensities are given by

$$I_{pp} = I(pp \to pK^{+}\Lambda) = \frac{1}{4} \sum_{\text{spins}} |\langle f | \mathcal{M}_{1} | i \rangle|^{2} = \frac{1}{4} \left(|W_{1,s}|^{2} + 2 |W_{1,t}|^{2} \right), \qquad (2.2)$$

$$I_{pn} = I(pn \to nK^{+}\Lambda) = I(pn \to pK^{0}\Lambda) = \frac{1}{16} \left(|W_{1,s}|^{2} + 2 |W_{1,t}|^{2} + |W_{0,t}|^{2} \right), \quad (2.3)$$

where there is no interference between the two isospin amplitudes due to the spin averaging.

One may expect that, close to threshold, the amplitudes $W_{i,s/t}$ should vary little, except for the different ΛN final-state interactions in the spin-singlet (s) and -triplet (t) systems. If we neglect these fsi, the corresponding total cross-section becomes

$$\sigma(pp \to pK^+\Lambda) = \frac{1}{256\pi^2 ps} \frac{(m_p m_A m_K)^{1/2}}{(m_p + m_A + m_K)^{1/2}} \times Q^2 I_{pp} ,$$
(2.4)

and similarly for the pn reaction. Here the m_i are the masses in the final state, p is the incident proton c.m. momentum, \sqrt{s} the total c.m. energy, and $Q = \sqrt{s} - \sum m_i$, the excess energy.

In the near-threshold region, both the proton analysing powers and the Λ polarisations should vanish:

$$\begin{aligned} \boldsymbol{A}_p &= \boldsymbol{0} \ , \\ \boldsymbol{P}_{\Lambda} &= \boldsymbol{0} \ . \end{aligned} \tag{2.5}$$

Only tensor combinations are predicted to be non-zero. Of these, the most "easily" accessible experimentally are the transverse spin-correlation (C_{NN}) and spin-transfer parameters (D_{NN}) , which are given by

$$\begin{split} I_{pp} C_{NN}(\vec{p} \, \vec{p} \to pK^{+}\Lambda) &= \frac{1}{4} |W_{1,s}|^{2} ,\\ I_{pn} C_{NN}(\vec{p} \, \vec{n} \to nK^{+}\Lambda) &= \frac{1}{16} \left(|W_{1,s}|^{2} - |W_{0,t}|^{2} \right) ,\\ I_{pp} D_{NN}(\vec{p} \, p \to pK^{+}\vec{\Lambda}) &= -\frac{1}{2} \operatorname{Re}(W_{1,s}W_{1,t}^{*}) ,\\ I_{pn} D_{NN}(\vec{p} \, n \to nK^{+}\vec{\Lambda}) &= -\frac{1}{8} \operatorname{Re}\left\{ (W_{1,s} + W_{0,t})W_{1,t}^{*} \right\} ,\\ I_{pn} D_{NN}(p\vec{n} \to nK^{+}\vec{\Lambda}) &= -\frac{1}{8} \operatorname{Re}\left\{ (W_{1,s} - W_{0,t})W_{1,t}^{*} \right\} . \end{split}$$

$$(2.6)$$

Since there are only five independent observables, there must be two relations among the above. The average of the polarisation transfers in pn collisions is proportional to that in the pp case. The other result is more interesting:

$$4I_{pn}\left[1+C_{NN}(\overrightarrow{p}\,\overrightarrow{n}\to nK^{+}\Lambda)\right] = I_{pp}\left[1+C_{NN}(\overrightarrow{p}\,\overrightarrow{p}\to pK^{+}\Lambda)\right], \qquad (2.7)$$

which means that, in the near-threshold region, the additional measurement of the spin correlation in np collisions would afford no further information. Alternatively, a



Fig. 1. Bare non-strange and strange one-meson–exchange contributions to the $pp \rightarrow pK^+\Lambda$ and $pn \rightarrow nK^+\Lambda$ amplitudes.

determination of the two spin correlations would be sufficient to fix $\mathcal{R}(K^+)$ without having to rely on cross-section information.

It must, however, be stressed that the measurement of the unpolarised cross-sections on the proton and neutron, plus the spin correlation on the neutron, and the spintransfer parameters in $\vec{p}p$ and $\vec{p}n$ collisions would allow one to extract the magnitudes of the three amplitudes and determine (up to two discrete ambiguities) the relative phases of $W_{1,s}$, $W_{1,t}$, and $W_{0,t}$ in a completely modelindependent way. Since this decomposition isolates particular spin states, it might permit the separate investigations of the ΛN spin-triplet and spin-singlet interactions.

3 One-boson–exchange models

Both strange and non-strange meson exchanges can contribute to $K^+\Lambda$ production in nucleon-nucleon collisions and the two sets of diagrams are illustrated on the leftand right-hand sides of fig. 1 before the inclusion of effects arising from the distortion of the initial and final waves.

Near threshold, the only significant energy variation is expected to arise from the spin-singlet and -triplet fsi enhancements. The relevant propagators, coupling constants, masses, etc. are evaluated at threshold and so merely contribute to the overall strength [6]. Employing the same technique and notation that we used for η production, we find that

$$W_{1,s} = 2\mathcal{B}_{\rho} + 2\mathcal{B}_{\omega} - \mathcal{D}_{\pi} - \mathcal{D}_{\eta} + \mathcal{D}_{K}^{1},$$

$$W_{1,t} = \mathcal{D}_{\pi} + \mathcal{D}_{\eta} + \mathcal{D}_{K}^{1},$$

$$W_{0,t} = 6\mathcal{B}_{\rho} - 2\mathcal{B}_{\omega} + 3\mathcal{D}_{\pi} - \mathcal{D}_{\eta} + \mathcal{D}_{K}^{0},$$
(3.1)

where $\mathcal{D}_{\pi,\eta}$ is the amplitude for the exchange of a pseudoscalar meson and $\mathcal{B}_{\rho,\omega}$ the dominant vector-exchange term. These amplitudes have the structure of an NNx coupling constant, the propagator for the meson x, followed by the final $xN \to K^+Y$ transition, which is dominated by the $S_{11}(1650)$ near threshold. The kaon exchange terms are similar, except that there is then an NAK coupling constant and two isospin possibilities in KN elastic scattering, leading to the two terms denoted here by \mathcal{D}_K^I . However, it has been pointed out by Laget [14] that the isoscalar K^+N scattering is dominantly p-wave and so would contribute relatively little here.

Though, for completeness, many terms have been included in eq. (3.1), we will concentrate our analysis on just those for π and ρ exchange. The η and K terms might be reduced in importance by the weak coupling constants and, for η production, ω exchange is reduced by the weak $\omega N \rightarrow S_{11}(1535)$ coupling.

Using vector dominance to estimate the $\rho N \rightarrow \eta N$ amplitudes, we predicted for η production that $\mathcal{D}_{\pi} \approx 0.7 \mathcal{B}_{\rho}$ [6], which led to a reasonable agreement with the large experimental value of $\mathcal{R}(\eta)$ [4]. To estimate the corresponding value for K^+ production, this π/ρ factor should be scaled by the ratio of the amplitudes for the production of K^+ with pion and photon beams:

$$\mathcal{D}_{\pi} \approx 0.7 \left(\frac{|f(\pi^- p \to K^0 \Lambda)|^2 |f(\gamma p \to \eta p)|^2}{|f(\pi^- p \to \eta n)|^2 |f(\gamma p \to K^+ \Lambda)|^2} \right)^{1/2} \mathcal{B}_{\rho},$$
(3.2)

where we have assumed that the same resonances are responsible for the production with pions and photons so that, in the absence of other interactions, the contributions are relatively real.

Taking the experimental data from refs. [21-24], we find that

$$\mathcal{D}_{\pi} \approx 0.7 \sqrt{\frac{(58 \pm 10)(4.6 \pm 0.2)}{(810 \pm 100)(0.19 \pm 0.04)}} \,\mathcal{B}_{\rho} = (0.9 \pm 0.2)\mathcal{B}_{\rho} \,.$$
(3.3)

4 The ΛN final-state interaction

To determine the overall normalisation of the $pp \rightarrow pK^+\Lambda$ cross-section, one would need reliable information on the Λp scattering wave functions, which is still sadly lacking [19]. However, the shape of the energy dependence is, to a large extent, fixed by just the Λp scattering lengths and effective ranges in the combination that gives the positions (ε) of the virtual bound states. The effect of the fsi on the shape of the cross-section can be included by



Fig. 2. Prediction for $\mathcal{R}(K^+)$ as a function of $\mathcal{D}_{\pi}/\mathcal{B}_{\rho}$, assumed to be real. Taking this value from eq. (3.3) leads to a ratio close to the maximum of 7.

multiplying the threshold value of I in eq. (2.4) by the factor [3]

$$\mathcal{Z} = \frac{4}{\left(1 + \sqrt{1 + Q/\varepsilon}\right)^2} \,. \tag{4.1}$$

A useful survey of theoretical and experimental information on the low-energy Λp parameters is provided in ref. [25]. An early experiment [26] suggested that the values for the triplet and singlet energies were quite close ($\varepsilon_t = 5.6$ MeV, $\varepsilon_s = 5.1$ MeV) but with large error bars. However, it has been shown [10] that the statistical average of these two ($\varepsilon_t = 5.5 \pm 0.6$ MeV) gives a good representation of the $pK^+\Lambda$ total cross-section data. Given the current theoretical uncertainty, for simplicity of presentation, we take $\varepsilon_s = \varepsilon_t$. Of course, once the two crosssections and one spin correlation have been measured, it might be possible to see the effects of the pole positions in well-identified spin states. The ΛN energy dependence of the spin-transfer coefficients would be sensitive to differences in scattering lengths.

5 Results

By taking $\varepsilon_s = \varepsilon_t$, it follows that $\mathcal{R}(K^+)$ should not depend upon the excitation energy Q and in fig. 2 the prediction for this has been drawn as a function of $x = \mathcal{D}_{\pi}/\mathcal{B}_{\rho}$, where it has been assumed that the π - and ρ -exchange amplitudes have the same phase.

As $x \to \infty$, $\mathcal{R}(K^+) \to 1$ [27], which is very different to the factor of five expected for η production under similar assumptions. This difference arises, in part, because we do



Fig. 3. Transverse spin-correlation C_{NN} (solid curve) and spin-transfer D_{NN} (broken curve) parameters for the $pp \rightarrow pK^+\Lambda$ reaction as functions of $\mathcal{D}_{\pi}/\mathcal{B}_{\rho}$, assumed to be real. Taking the value of this from eq. (3.3) leads to a large negative D_{NN} , without invoking kaon exchange [14].

not include the contribution of the K^0 in the definition of \mathcal{R} , but also because the $W_{1,t}$ term is forbidden by the Pauli principle for the $pp \to pp\eta$ reaction. On the other hand, pure ρ exchange leads to $\mathcal{R}(K^+) = 2.5$ and for a wide range of x the ratio is well over unity. It is interesting to note that the figure of 0.9, resulting from the crude scaling model of eq. (3.3), corresponds almost to the peak value of 7 shown in fig. 2.

From eqs. (2.6) and (3.1), it is seen that, with this value of x, one expects $C_{NN}(pp \rightarrow pK^+A) = 0.43$, to be contrasted with the 0.5 and 1.0 expected for pure π and ρ exchange, respectively. The variation of both C_{NN} and D_{NN} with x is shown in fig. 3, where it is seen that D_{NN} has an even more interesting behaviour, with a minimum of about -0.7 for x = 0.9. This is to be contrasted with the +2/3 and 0 expected for pure π and ρ exchange, respectively.

6 Conclusions

We have studied the charge and spin dependence of the $pp \rightarrow pK^+\Lambda$ total cross-section near threshold in the region where the final particles are in relative S-states. The overall cross-section strength is hard to estimate with any confidence, due principally to the poor knowledge of the ΛN potential. Scaling the cross-section from that for η production by using the Bargmann potential, as in ref. [15], avoids some of the uncertainties associated with the initial-state interactions [8], though the threshold energy for K^+ production is a little higher than for the η . Despite the good Q-dependence, it leads to an estimate that is too low by a factor of up to five. This probably indicates that the short-range part of the Λp interaction is less repulsive than that for pp [19].

Since there are only three amplitudes describing $K^+\Lambda$ production on the proton and neutron near threshold, it is clear that there should be some model-independent relations between the charge and spin dependence of the observables. To go further than this, we have worked in a simplified meson-exchange model where, for simplicity, the amplitudes have been assumed to be in phase. Keeping only the π and ρ terms, and scaling their relative strength from that found for η production, we find that production of $K^+\Lambda$ on the neutron could indeed be much stronger than on the proton. However, the prediction does depend upon cancellations and is far less robust than that in the η case.

The spin-correlation and -transfer parameters are also expected to depend sensitively upon x, the relative π/ρ strength. Of especial interest is D_{NN} which, though +2/3 for π exchange and 0 for ρ exchange, is predicted to be strongly negative for our preferred value of x though, since this reflects an interference, the exact value will be affected by phase shifts coming from distortions in the initial state. The negative value found for D_{NN} in $pp \rightarrow pK^+\Lambda$ in different kinematic conditions away from threshold by the DISTO group [28] was taken as evidence for the dominance of kaon over pion exchange [14], but it is important to stress that the possibility of ρ exchange was not considered by these authors.

From measurement of C_{NN} in pp collisions, as well as the pn and pp cross-section, one could separate the magnitudes of the W amplitudes. This might permit the investigation of the ΛN final-state interaction in definite spin states. Furthermore, within the π/ρ model, such measurements would allow one to predict the spin-transfer coefficient D_{NN} , though at that stage it would be important to include phases associated with initial-state interactions. This would then show whether or not other exchanges are important for threshold kaon production.

This work was initiated through discussions with V. Koptev and Y. Valdau during a Royal Society sponsored visit by one of the authors (C.W.) to the Petersburg Nuclear Physics Institute. The authors are very grateful for constructive comments from C. Hanhart and A. Gasparyan.

References

- 1. P. Moskal et al., Prog. Part. Nucl. Phys. 49, 1 (2002).
- 2. C. Hanhart, Phys. Rep. 397, 155 (2004).
- 3. G. Fäldt, C. Wilkin, Phys. Lett. B 382, 209 (1996).
- 4. H. Calén et al., Phys. Rev. C 58, 2667 (1998).
- 5. J.-F. Germond, C. Wilkin, Nucl. Phys. A 518, 308 (1990).
- 6. G. Fäldt, C. Wilkin, Phys. Scr. 64, 427 (2001).
- K. Nakayama, J. Speth, T.S.H. Lee, Phys. Rev. C 65, 045210 (2002).
- 8. V. Baru et al., Phys. Rev. C 67, 024002 (2003).
- J.T. Balewski *et al.*, Phys. Lett. B **388**, 859 (1996);
 J.T. Balewski *et al.*, Phys. Lett. B **420**, 211 (1998); S. Sewerin *et al.*, Phys. Rev. Lett. **83**, 682 (1999).
- 10. P. Kowina et al., Eur. Phys. J. A 22, 293 (2004).
- 11. R. Bilger et al., Phys. Lett. B 420, 217 (1998).
- W. Schroeder, Eur. Phys. J. A 18, 347 (2003); W. Schroeder, PhD Thesis, University of Erlangen (2003).
- 13. Y. Valdau, Int. J. Mod. Phys. A 20, 677 (2005).
- 14. J.M. Laget, Phys. Lett. B 259, 24 (1991).
- 15. G. Fäldt, C. Wilkin, Z. Phys. A 357, 241 (1997).
- 16. K. Tsushima et al., Phys. Rev. C 59, 369 (1999).
- R. Shyam, Phys. Rev. C 60, 055213 (1999); arXiv:hepph/0406297.
- 18. A. Gasparian et al., Phys. Lett. B 480, 273 (2000).
- Th.A. Rijken, V.G.J. Stoks, Y. Yamamoto, Phys. Rev. C 59, 21 (1999).
- See, for example, H. Pilkuhn, *The Interactions of Hadrons* (North-Holland, Amsterdam, 1967).
- 21. D.M. Binnie et al., Phys. Rev. D 8, 2789 (1973).
- 22. L. Tiator et al., Phys. Rev. C 60, 035210 (1999).
- J.J. Jones *et al.*, Phys. Rev. Lett. **26**, 860 (1971);
 R.D. Baker *et al.*, Nucl. Phys. B **141**, 29 (1978).
- 24. K.-H. Glander et al., Eur. Phys. J. A 19, 251 (2004).
- 25. F. Hinterberger, A. Sibirtsev, Eur. Phys. J. A 21, 313 (2004).
- 26. G. Alexander et al., Phys. Rev. 173, 1452 (1968).
- 27. A. Gasparyan, private communication.
- 28. F. Balestra et al., Phys. Rev. Lett. 83, 1534 (1999).